$\qquad$

Graphs of Polynomial Functions NOTES

| Finding the End Behavior of a function |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Degree | Leading Coefficient | Graph Comparison |  | End Behavior |
| Even | Positive | $y=x^{2} \bigsqcup$ | Rise right <br> Rise left | $\begin{aligned} & \text { As } x \rightarrow+\infty, f(x) \rightarrow+\infty \\ & \text { As } x \rightarrow-\infty, f(x) \rightarrow+\infty \end{aligned}$ |
| Even | Negative |  | Fall right <br> Fall left | $\begin{aligned} & \text { As } x \rightarrow+\infty, f(x) \rightarrow-\infty \\ & \text { As } x \rightarrow-\infty, f(x) \rightarrow-\infty \end{aligned}$ |
| Odd | Positive | $y=x^{3}$ | Rise right <br> Fall left | $\begin{aligned} & \text { As } x \rightarrow+\infty, f(x) \rightarrow+\infty \\ & \text { As } x \rightarrow-\infty, f(x) \rightarrow-\infty \end{aligned}$ |
| Odd | Negative | $y=-x^{3}$ | Fall right <br> Rise left | $\begin{aligned} & \text { As } x \rightarrow+\infty, f(x) \rightarrow-\infty \\ & \text { As } x \rightarrow-\infty, f(x) \rightarrow+\infty \end{aligned}$ |

## Turning Points

A polynomial function has a degree of $\boldsymbol{n}$.
Maximum Number of Turning Points $=\boldsymbol{n} \mathbf{- 1}$

## Steps for Graphing a Polynomial Function

1. Find the real zeros and $y$-intercept of the function.
2. Plot the $x$ - and $y$-intercepts.
3. Make a table for several $x$-values that lie between the real zeros.
4. Plot the points from your table.
5. Determine the end behavior of the graph.
6. Sketch the graph.

## Multiplicity

The multiplicity of root $r$ is the number of times that $x-r$ is a factor of $P(x)$.

Odd Multiplicity
The graph of $P(x)$ crosses the $x$-axis.
Even Multiplicity
The graph of $P(x)$ touches the $x$-axis, but does not cross it. (i.e. U-turn)


Root $\boldsymbol{b}$ has odd multiplicity
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## Graphs of Polynomial Functions NOTES

Complete the table to identify the leading coefficient, degree, and end behavior of each polynomial.

|  | Polynomial | Leading <br> Coefficient | Degree | Graph <br> Comparison | End Behavior |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 1. | $f(\mathrm{x})=4 x^{7}+5 x^{4}+2$ |  |  |  |  |
| 2. | $f(\mathrm{x})=-7 x^{6}+2 x^{2}-3 x$ |  |  |  |  |
| 3. | $f(\mathrm{x})=-2 x^{5}-x^{3}+6 x$ |  |  |  |  |

4. Identify whether each function graphed has an odd or even degree and a positive or negative leading coefficient.


Degree: $\qquad$
Leading Coefficient: $\qquad$ _



Degree: $\qquad$
Leading Coefficient: $\qquad$ -


Degree: $\qquad$
Leading Coefficient: $\qquad$ -
$\qquad$
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| Equation | Solution (zeros) | $x$-int. | Multiplicity for each zero | $\begin{gathered} \text { Graph at } \\ x \text {-axis } \\ (\text { Use BOX 1) } \end{gathered}$ | End Behavior | Maximum number of turning points |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| \#5 $P(x)=(x-1)^{2}(x-3)$ |  |  |  |  | Degree $=$ $\qquad$ <br> Leading Coefficient = $\qquad$ <br> Graph Comparison (circle one) $y=x^{2} / y=-x^{2} / y=x^{3} / y=-x^{3}$ <br> End Behavior (Use BOX 2): $\qquad$ |  |
| \#6 $P(x)=\frac{1}{12}(x+2)^{2}(x-3)^{2}$ |  |  |  |  | Degree $=$ $\qquad$ <br> Leading Coefficient $=$ $\qquad$ <br> Graph Comparison (circle one) $y=x^{2} / y=-x^{2} / y=x^{3} / y=-x^{3}$ <br> End Behavior (Use BOX 2): $\qquad$ |  |
| \#7 $P(x)=x(x-3)(x+2)$ |  |  |  |  | Degree $=$ $\qquad$ <br> Leading Coefficient $=$ $\qquad$ <br> Graph Comparison (circle one) $y=x^{2} / y=-x^{2} / y=x^{3} / y=-x^{3}$ <br> End Behavior (Use BOX 2): $\qquad$ |  |

Determine if the graphs do one of the following at the given $\boldsymbol{x}$-intercepts.
BOX 1 A: The graph crosses the $x$-axis at the $x$-intercept. (ODD MULTIPLICITY)
B: The graph touches the $x$-axis and turns around at the $x$-intercept. (EVEN MULTIPLICITY)

## End Behavior

BOX 2
C: As $x \rightarrow+\infty, f(x) \rightarrow+\infty \quad$ (Rises Right) $\quad \mathrm{E}:$ As $x \rightarrow+\infty, f(x) \rightarrow-\infty \quad$ (Falls Right)
$\mathrm{D}:$ As $x \rightarrow-\infty, f(x) \rightarrow+\infty \quad$ (Rises Left)
F: As $x \rightarrow-\infty, f(x) \rightarrow-\infty \quad$ (Falls Left)
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Graphs of Polynomial Functions NOTES

$$
\text { \#5 } \quad \text { Graph } P(x)=(x-1)^{2}(x-3)
$$


\#7 Graph $P(x)=x(x-3)(x+2)$

\#6 $\quad$ Graph $\quad P(x)=\frac{1}{12}(x+2)^{2}(x-3)^{2}$

$y$-intercept

Additional Points
$y$-intercept

Additional Points

